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## DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY/MANAGEMENT/ COMMERCIAL PRACTICE, APRIL - 2023

### **MATHEMATICS - II**

[Maximum marks: 75] (Time: 3 Hours)

#### **PART A**

I. Answer all the following questions in one word or one sentence. Each question carries 1 mark

		$(9 \times 1 = 9 \text{ Marks})$	
		Module outcome	Cognitive level
1	Evaluate $\begin{vmatrix} 3 & 4 \\ -2 & 3 \end{vmatrix}$	M1.01	R
2	Find $A^{T}$ if $A = \begin{bmatrix} 1 & 3 & 5 \\ 3 & 4 & 2 \\ 2 & 1 & 3 \end{bmatrix}$	M1.03	R
3	Find $\vec{a} + \vec{b}$ if $\vec{a} = 3\hat{i} + 4\hat{j} - 2\hat{k}$ , $\vec{b} = 2\hat{i} - 3\hat{j} - 2\hat{k}$	M2.02	U
4	Find a vector joining $(1,2,-3)$ and $(3,1,1)$	M2.01	R
5	$\int sec^2x.dx =$	M3.01	R
6	Find $\int (2x+3)dx$	M3.01	U
7	Find $\int x^5 dx$	M3.01	U
8	Find order and degree of the differential equation $\left(\frac{dy}{dx}\right)^3 + \frac{d^2y}{dx^2} = 1$	M4.02	A
9	Write the formula for finding area included between the curve $y = f(x)$ ,	M4.01	R
	X – axis, and the ordinates at $x = a$ and $x = b$		

#### **PART B**

II. Answer any eight questions from the following. Each question carries 3 marks.

 $(8 \times 3 = 24 \text{ Marks})$ 

		Module outcome	Cognitive level
1	Solve for x, if $\begin{vmatrix} 3x & 7 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} 4 & 2 \\ 2 & 2 \end{vmatrix}$	M1.01	U
2	If $A = \begin{bmatrix} 3 & -2 \\ -7 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & -3 \\ 3 & 2 \end{bmatrix}$ , Compute 3A - 5B.	M1.03	U
3	If $A = \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix}$ , $B = \begin{bmatrix} -1 & 2 \\ 2 & 1 \end{bmatrix}$ , $C = \begin{bmatrix} 3 & -2 \\ 1 & 3 \end{bmatrix}$ Compute (A+B)C.	M1.03	R
4	Find dot product and angle between the vectors.	M2.02	R
	$\vec{a} = \hat{\imath} - 2\hat{\jmath} + 3\hat{k}$ and $\vec{b} = 3\hat{\imath} - 2\hat{\jmath} + \hat{k}$		
5	Find $\vec{a} \times \vec{b}$	M2.02	U
	$\vec{a} = 3\hat{i} + \hat{j} - 2\hat{k}$ and $\vec{b} = \hat{i} - 3\hat{j} + 4\hat{k}$		
6	Find $\int \sin 2x \cdot \cos 3x \cdot dx$	M3.01	R
7	Find $\int \tan x  dx$	M3.02	U

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8	Find $\int \frac{2+\sin x}{\cos^2 x} dx$	M3.01	R
9	Find area bounded by the curve = $x + \sin x$ , the X- axis and the ordinates at $x = 0$ and $x = \frac{\pi}{2}$	M4.01	A
10	Solve $\frac{dy}{dx} = 2y$	M4.02	A

# PART C Answer all questions. Each question carries seven marks

 $(6 \times 7 = 42 \text{ Marks})$ 

			$(6 \times 7 = 42 \text{ Marks})$		
			Module outcome	Cognitive level	
III	Solve the following system of equation using Cramer's rule	( <b>-</b> )	M1.02	U	
	x + y + z = 3, $2x + 3y + z = 6$ , $x - y - z = -3$	(7)			
IV	OR Solve the following system of equation value inverse of		M1.03	U	
1 V	Solve the following system of equation using inverse of coefficient matrix $5x - y = 3.4x + 2y = -1$	(7)	W11.03	U	
	Coefficient matrix $3x - y - 3$ , $4x + 2y - 1$	(7)			
V	(a) If A,B,C are three points whose position vectors are given by		M2.02	U	
	$A(\hat{i}+3\hat{j}+2\hat{k})$ , $B(2\hat{i}-\hat{j}+\hat{k})$ and $C(2\hat{i}-3\hat{j}+4\hat{k})$ , Find $\overrightarrow{AB}$ x $\overrightarrow{AC}$	(4)			
	(- · · · · · · · · · · · · · · · · · ·	( ')			
	(b) Find the work done in moving an object along the vector			U	
	$3\hat{i} + 2\hat{j} - 5\hat{k}$ if the force applied is $5\hat{i} + 4\hat{j} + \hat{k}$ .	(3)	M2.03	S	
	OR		M2.02		
VI	(a) Find a unit vector perpendicular to both		1012.02	U	
	$\vec{a} = 2\hat{\imath} + 2\hat{\jmath} + \hat{k}$ and $\vec{b} = 6\hat{\imath} - 3\hat{\jmath} + 2\hat{k}$ .	(5)		**	
	(b) Prove that $\vec{a} = 3\hat{i} - \hat{j} + 2\hat{k}$ and $\vec{b} = 2\hat{i} + 2\hat{j} - 2\hat{k}$ are perpendicular	r.(2)	M2.02	U	
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VII	(a) Find the value of p so that $p\hat{i} + 2\hat{j} + 3\hat{k}$ and $-\hat{i} + 3\hat{j} - 4\hat{k}$ are	(2)	M2.02	R	
	Perpendicular.	(3)			
	(b) Find unit vector in the direction of $\vec{a} + \vec{b}$ if $\vec{a} = 2\hat{i} + 2\hat{j} - 5\hat{k}$ ,		M2.01	R	
	$\vec{b} = 2\hat{\imath} + \hat{\jmath} + 3\hat{k}$	(4)	1412.01	K	
	OR				
VIII	(a) Find moment about the point $\hat{i} - 3\hat{j} + \hat{k}$ of a force $4\hat{i} - 3\hat{k}$ acting		M2.03	A	
	through the point $2\hat{i} - 2\hat{j} + 5\hat{k}$ .	(5)			
	(b) If the position vector of A is $2\hat{i} - \hat{j} - \hat{k}$ and position vector				
	of B is $-\hat{i} - 3\hat{j} + 3\hat{k}$ . Find $\overrightarrow{AB}$ .	(2)	M2.01	R	
IX	(a)Evaluate $\int \frac{\sec^2 x}{\sqrt{1-\tan^2 x}} . dx$	(4)	M3.02	U	
	(a) Evaluate $\int \frac{1}{\sqrt{1-tan^2x}} dx$	(4)			
	(b) Example 1 ( $\alpha + 1$ ) ( $\alpha + 2$ ) de	(2)			
	(b)Evaluate $\int (x+1) \cdot (x+2) dx$ . <b>OR</b>	(3)	M3.01	R	
X	(a)Evaluate $\int_0^4 x \sqrt{x^2 + 9}  dx$	(4)		T.T.	
	(a)Evaluate $\int_0^\infty x \sqrt{x^2 + 9} \cdot ax$	(4)	M3.03	U	
	(b) Evaluate $\int x^2 \log x  dx$	(2)	M3.02	U	
	(b)Evaluate $\int x^2 \cdot \log x \cdot dx$	(3)		O	

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XI	(a)Evaluate $\int_{1}^{2} \log x \cdot dx$	(4)	M3.03	U
	(b)Evaluate $\int \cos 4x \cdot \sin 2x \cdot dx$	(3)	M3.02	R
XII	OR (a)Evaluate $\int \cos^2 2x \cdot dx$	(3)	M2.01	R
	(b)Evaluate $\int_{1}^{2} \frac{2x+1}{x^2+x+1} dx$	(4)	M2.03	U
XIII	(a) Find the area bounded by the portion of the parabola $y^2 = 4x$ about the X- axis between the ordinates at $x = 0$ and $x = 4$ .	(3)	M4.01	A
	(b) Solve $dy = e^{3x + y} dx$	(4)	M4.02	A
	OR			
XIV	(a) Solve $\frac{dy}{dx} + 2y \tan x = \sin x$ (b) Solve $\frac{dy}{dx} = 2$	(5)	M4.02	A
	(b) Solve $\frac{dy}{dx} = 2$	(2)	M4.02	A

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